On the degree of the Gauss map for the Theta Divisor of a Prym

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It will be briefly discussed the stratification of the moduli space \mathcal{A}_g , (of principally polarized abelian varieties (A, Θ) of dimension g), by the degree of the Gauss map for the theta divisor Θ . Then some geometric descriptions of the Gauss map for the theta divisor of a Prym variety (P, Ξ) will be considered. In particular, if (P, Ξ) is the Prym defined by the étale double covering $\pi : \tilde{C} \to C$, there will be some emphasys on the relations between Ξ and the family of rank three quadrics touching the canonical model of the curve C. These relations will be used to compute the degree of the Gauss map in the case of a general Prym variety, which is

$$2^{g-3} + D(g)$$

where D(g) is the degree of the variety parametrizing quadrics of P^{g-1} having rank ≤ 3 , $(g-1 = dimP, g \geq 3)$. Some special examples and some other possible combinatorial interpretations of this number will be discussed.