Seshadri constants and symbolic powers

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I will discuss recent work related to a question of Craig Huneke. Huneke asked if J^2 contains $J^{(3)}$ whenever J is a radical ideal defining a finite subscheme of $\mathbb{P}^2$. I will suggest a generalization for $\mathbb{P}^N$. In case J defines a finite set of generic points I will relate the problem to Seshadri constants and outline an approach to a proof. (In case $N = 2$, the approach works and thus J^2 contains $J^{(3)}$ whenever J is a radical ideal defining any finite set of generic points of $\mathbb{P}^2$.)