The neural mechanisms of dynamic decisions

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University of Barcelona Spring Seminar Series in Theoretical Neuroscience April 25, 2023

Outline

- Quantitative models of decisions
 - The drift-diffusion model: a good foundation
 - How we can/should move beyond it
- What is the evidence to help us decide between models?
 - Behavioral studies
 - Neural recording studies
- Broader implications
 - Individual differences
 - Pathological conditions

Random dot motion discrimination task



Gold & Shadlen (2007) Annual Reviews in Neuroscience

Which way are the dots moving?

How do you make decisions over time?

- The "Drift-diffusion model" (DDM) Ratcliff (1978) Psychological Review
 - Hypothesis: Deliberation is similar to a random walk to a threshold



- Some noisy neural variable (x) is changing over time, biased by sensory information, until it crosses a decision threshold
 - The strength of the evidence determines the rate of drift
 - Any prior information determines the starting point
 - The desired accuracy determines the threshold

The Drift-Diffusion Model (DDM)

An integrator of evidence to a constant threshold



DDM ≈ sequential probability ratio test

 If you want to achieve a given level of accuracy α (e.g. 95%), how many samples should you take from the world before you commit to choice A or B?

 χ

$$x_A(n) = \log \frac{p(A|s_1...s_n)}{p(B|s_1...s_n)} < \log \frac{\alpha}{1-\alpha}$$

• From Bayes' Rule:

$$A(n) = \log \frac{p(A)}{p(B)} + \sum_{k=1}^{n} \log \frac{p(s_k|A)}{p(s_k|B)} < \log \frac{\alpha}{1-\alpha}$$

prior accumulated
evidence
(sum of log-likelihood ratios)

 $x_A(t) = Z_A + \int_0^t E_A(\tau) d\tau < T$

 Integration of evidence to a threshold implements the decision policy that optimizes time for any desired accuracy

Behavioral evidence for the DDM



- Because of noise, the process will create RT distributions
 - Weaker sensory evidence, later decisions and broader distributions
- This is well-supported by behavioral data from many decision tasks

Neural evidence for the DDM



Roitman & Shadlen (2002) J. Neurosci.

- Neural activity in the lateral intraparietal area (LIP) grows at a rate related to the strength of evidence for a cell's preferred target
- Activity reaches a similar level just before the saccade
- Conclusion: LIP represents the integrated motion signal

The Drift-Diffusion Model (DDM)

An integrator of evidence to a constant threshold



- The diffusion model is widely accepted as the explanation for decision-making during perceptual discrimination tasks
 - Makes good mathematical sense
 - Explains behavioral data on accuracy and RT distributions
 - Explains the widespread build-up of neural activity during decisions

However...

- 1. What if the world changes?
- 2. What do we want to integrate?
- 3. What do we want to optimize?

Q1: What if the world changes?

 During natural behavior, the world is always changing

- Any integrator will be sluggish in its response to such changes
- Need to be able to quickly respond to changes
 - Reset?
 - Sudden increase in gain?
 - Some other mechanism?



Q2. What *should* be integrated?

$$\log \frac{p(A)}{p(B)} + \sum_{k=1}^{n} \log \frac{p(s_k|A)}{p(s_k|B)} < \log \frac{1-\alpha}{\alpha}$$

This assumed that sequential samples are statistically independent

- But that is not true in general. If you're looking at the same stimulus, later samples are partially or completely *redundant*
- To take this redundancy into account, we need to extend Bayes' Rule to k+1 variables, yielding:

$$\log \frac{p(A)}{p(B)} + \sum_{k=1}^{n} \log \frac{p(s_k | A, s_1, \dots, s_{k-1})}{p(s_k | B, s_1, \dots, s_{k-1})} < \log \frac{1 - \alpha}{\alpha}$$

- If sample s_k is completely independent of previous samples, then $p(s_k|X, s_1, ..., s_{k-1}) = p(s_k|X)$, and this reduces to the equation on top i.e. you should sum independent samples
- If sample s_k is completely predicted by previous samples, then $p(s_k|X, s_1, ..., s_{k-1}) = 1$, and $\log \frac{1}{1} = 0$

i.e. you should ignore redundant samples

So what should we accumulate?

Should we accumulate *all* evidence?

$$\log \frac{p(A)}{p(B)} + \sum_{k=1}^{n} \log \left(\frac{I_{k|A}}{I_{k|B}} \times \frac{p(s_k|A)}{p(s_k|B)} \right)$$

 $I_{k|X} = \frac{p(s_1, \dots, s_{k-1}, s_k|X)}{p(s_1, \dots, s_{k-1}|X)p(s_k|X)}$

related to the mutual information between sample *k* and previous ones

- <u>Conclusion</u>: We should only accumulate evidence to the extent that it is *novel*
- i.e. In order to properly implement the SPRT, we have to take statistical dependence between samples into account
- Ex: buying newspapers

What's optimal vs. possible vs. reasonable?

- Ideal mechanism: Compute the degree to which each sample contributes novel information
- <u>Another approach</u>: Try predicting the next sample and accumulate that which you can't predict
- <u>Simple 1st-order approximation</u>:
 - Novelty = change from previous sample
 - Assume fluctuations above a certain frequency are just noise
 - Low-pass filter









In a noisy task





- First sample is independent
- Second gives some uncorrelated novel evidence
- Third sample gives less
- Etc.
- The integral... ...looks like a low-pass filter

Leaky integration

- Accumulation of novelty will look like a low-pass filter
 - Leaky Competing Accumulator (Usher & McClelland, 2001)
- But then how do you get to the threshold?



Q3: What kind of optimality do we want?

- If you're doing statistics then what you care about is *accuracy*
 - The criterion of desired accuracy is determined by convention
 - p<0.05 = 95% confidence in your result
 - p<0.01 = 99% confidence in your result
 - The SPRT is optimal in that it minimizes the time required to reach that level of accuracy
 - If results not significant, get more data, even if it takes you another year to finish your thesis...
- But what if you're an animal in the wild?
 - Suppose you've reached 93% confidence
 - Do you wait to reach 95%?
 - What if it would take another thirty minutes?
 - What if it would take a year?
 - Time runs out, opportunities are lost, predators come and eat you!
 - You want to optimize *reward rate*

Reward rate

Reward Rate

$$RR = \frac{p(t) \cdot U - C}{t + m + d}$$

- where
 - p(t) is the probability of achieving a favorable outcome
 - t is the time spent deciding and planning
 - U is the subjective utility of that outcome
 - *C* is the subjective cost of trying (including "opportunity cost")
 - m is the time spent moving
 - *d* is the delay before you can try again
- "Time-discounted expected value"
- Similar form as "harvest intake" in foraging (Charnov, 1976)

Assumptions



- 1. The probability of achieving a favorable outcome improves with time
- 2. But with diminishing returns

Therefore, the expected reward rate has a peak

- The peak of reward rate occurs when RR'(t) = 0 and RR''(t) < 0, or when $p(t) = p'(t)(t + m + d) + \frac{C}{H}$
- This is the best time to commit



Geometric interpretation $p(t) = p'(t)(t + m + d) + \frac{C}{U}$



A dropping accuracy criterion

- The accuracy criterion drops, so ۲ you always reach it eventually
- But neural data suggests the ۲ threshold is constant





Q1: What if the world changes?

 During natural behavior, the world is always changing

- Any integrator will be sluggish in its response to such changes
- Need to be able to quickly respond to changes
 - Reset?
 - Sudden increase in gain?
 - Some other mechanism?



A low-pass filter has a short time constant – it responds to changes quickly

Two models

- Drift-diffusion model (DDM)
 - Integrate all samples
 - Stop at a constant criterion
- Urgency-gating model (UGM)
 - Integrate novel information (e.g. low pass filter)
 - Urgency pushes activity to threshold, implementing a dropping criterion
- Similar but different
 - Both "rise to threshold"
 - Different mechanisms responsible for build-up



A space of models



But what about all that data?

• Nearly all experiments have used constant-evidence $E_A(t) = E_A$

t

- In those conditions
 - Diffusion model:

$$x_A(t) = \int_0^t E_A(\tau) d\tau$$
$$x_A(t) = \int_0^t E_A d\tau = E_A \int_0^t d\tau$$
$$x_A(t) = E_A t$$

- Urgency-gating: $x_A(t) = F[E_A(t)] \cdot u(t)$

$$x_A(t) = E_A \cdot u(t)$$

$$x_A(t)=E_A t$$

- Both make similar predictions at the behavioral and neural level
- To distinguish the models, need tasks with *changing evidence*

A space of models



Noisy motion with pulses

Carland, Marcos, Thura, & Cisek (2016) Journal of Neurophysiology





Matt Carland

Encarni Marcos



- Random dot motion discrimination task ۲
 - Reaction time version
 - Low stimulus coherence (3%)
 - We add brief pulses of extra motion at different times during the trial
- Diffusion model predictions ۲
 - Fast (low threshold): early pulses have an effect but late pulses are too late
 - Slow (high threshold): all pulses have an effect
- Urgency-gating model predictions ۲
 - Fast (high urgency): early pulses have an effect but late pulses are too late
 - Slow (low urgency): late pulses have an effect but early pulses "leak out"
- Test subjects in fast and slow conditions

How to get subjects to slow down?

- Instruction is always the same:
 - "Indicate motion as soon as you see it"
- Two kinds of trials:
 - Constant Motion Discrimination (CMD) trials, with and without pulses
 - Variable Motion Discrimination (VMD) trials, with changing evidence (3% coherence step every 200ms)
 - In VMD trials, motion is sometimes stronger if you wait

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- Design:
 - **Blocked**: Just CMD trials
 - Interleaved: Identical CMD trials are interleaved with VMD trials
- <u>Question</u>: Do subjects slow down in CMD trials when they're interleaved with VMD?





Do subjects slow down?



Mean RT, no-pulse trials, blocked condition (ms)

 Yes, 42/44 subjects are significantly slower on nopulse trials during the interleaved sessions

• <u>Question</u>: Does the effect of pulses in CMD trials change between conditions?

Results: Subject "JM"



- Blocked (fast) condition
 - Pulses at 100 and 200ms have a significant effect
 - Pulse at 400ms does not
 - Consistent with both models
 - Consistent with previous studies of motion pulses (Huk & Shadlen 2005; Kiani et al. 2008)
- Interleaved (slow) condition
 - Pulse at 400ms has a significant effect
 - Pulses at 100 and 200ms
 do not have an effect
 - Suggests strong leak
 Time constant of 100-250ms

Results: Fast subgroup



- Blocked (fast) condition
 - Pulses at 100 and 200ms have a significant effect
 - Pulse at 400ms does not

- Interleaved (slow) condition
 - Pulses at 200ms and 400ms have a significant effect
 - Pulse at 100 *does not* have a significant effect

Results: Slow subgroup



- Blocked (fast) condition
 - No effect of pulses

- Interleaved (slow) condition
 - No effect of pulses

Results: Subject "JM"



- Blocked (fast) condition
 - Pulses at 100 and 200ms have a significant effect
 - Pulse at 400ms does not
 - Consistent with both models
 - Consistent with previous studies of motion pulses (Huk & Shadlen 2005; Kiani et al. 2008)
- Interleaved (slow) condition
 - Pulse at 400ms has a significant effect
 - Pulses at 100 and 200ms
 do not have an effect
 - Suggests strong leak
 Time constant of 100-250ms

Individual RT-dependent trends



<u>Predict</u>: The time window in which a pulse is effective should depend on an individual's reaction time

Individual RT-dependent trends



Modeling with UGM & DDM



<u>Claim</u>: This result cannot be explained with the DDM, regardless of parameter settings
Task-dependence?

- "Two-model solution"
 - Use DDM when doing a "constant evidence" task
 - Use UGM when doing a "changing evidence" task
- Lacks parsimony
 - Use model X to explain data set A, and model Y for data set B...
 - ...but model Y already explains *both* data sets A and B
- Goodness of fit?
 - Hawkins et al. 2015, 2016 suggest DDM fits better than UGM in constant-evidence tasks (but don't test changing-evidence tasks)
 - A two-model solution includes parameters of both models, plus a switching mechanism
 - The fit to any given data set must be penalized for all of these parameters, including those of the "unused model"

A space of models



Conclusion, so far

- The "urgency-gating model" offers a better explanation of decision-making than the "drift-diffusion model"
 - Theoretically (considers redundancy, maximizes reward rate)
 - Empirically (fits a larger class of experiments)

(some confessions)

- Where do we go from here?
 - Neural mechanisms
 - Broader phenomena

Neural mechanisms

Can we find the neural correlates of evidence, urgency, and the mechanism of commitment?

The "tokens task"



David Thura



The "tokens task"



David Thura





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The "tokens task"

David Thura

$$p(R \mid N_R, N_L, N_C) = \frac{N_C!}{2^{N_C}} \sum_{k=0}^{\min(N_C, 7-N_L)} \frac{1}{k!(N_C - k)!}$$



Time



The "tokens task"

David Thura

$$p(R \mid N_R, N_L, N_C) = \frac{N_C!}{2^{N_C}} \sum_{k=0}^{\min(N_C, 7-N_L)} \frac{1}{k!(N_C - k)!}$$





Time



Thura, Cos, Trung & Cisek (2014) J. Neurosci.

- In easy trials, monkeys respond more quickly than in ambiguous or misleading trials
- In longer trials, decisions are made at a lower level of probability
 - Monkeys drop their accuracy criterion over time





Deriving the urgency signal



Ignasi Cos

David Thura

- For each trial, calculate the evidence available at the time the monkey made his decision
- Group trials according to decision time, and calculate the mean
- Dropping accuracy criterion = urgency signal
- Find *m* and *b* that provide the best fit



Thura, Cos, Trung & Cisek (2014) J. Neurosci.



The "tokens task"

David Thura







Time

Do monkeys adjust their behavior?



Do monkeys adjust their behavior?



Thura, Cos, Trung & Cisek (2014) J. Neurosci.



Urgency is context-dependent



- We derive distinct urgency functions for the two blocks
- Fast starts higher than Slow, and they converge over time

Thura, Cos, Trung & Cisek (2014) J. Neurosci.





M1 PMd

In "output regions", we predict an influence of both evidence and urgency



Thura & Cisek (2014) Neuron

The influence of "urgency"





Deriving the urgency signal from neural data



Thura & Cisek (2016) J. Neurosci.



Thura & Cisek (2014) Neuron; Thura & Cisek (in prep)

Brief detour

Reward rate

$$RR = \frac{p(t) \cdot U - C}{(t+m) + d}$$

- It also depends on movement time m
 - If you take more time to decide, you can save time by moving faster
 - If you took a guess, less need for accuracy
- Effort is a function of speed
 - Predict correlations between urgency and vigor



Yoon, Geary, Ahmed, Shadmehr (2018) PNAS

Correlation between urgency and vigor



Proposal: The level of urgency at time of decision influences the vigor of action

Basal Ganglia?



Thura & Cisek (2014) Neuron; Thura & Cisek (2016) J. Neurosci.; Thura & Cisek (2017) Neuron





Thura & Cisek (2014) Neuron; Thura & Cisek (2016) J. Neurosci.; Thura & Cisek (2017) Neuron





Thura & Cisek (2014) Neuron; Thura & Cisek (2016) J. Neurosci.; Thura & Cisek (2017) Neuron Thura & Cisek (2020) J. Neurophys.

Summary so far



Proposal:

Commitment occurs when the recurrent dynamical system (PMd/M1 ↔ BG) falls into an "attractor"

- Deliberation as competition
 - Potential actions from dorsal stream
 - Competition in PPC/PMd/M1
 - Evidence from dIPFC
 - Urgency from BG
- Cortex develops a contrast
 - Starts to spill into GPe
 - Reaches critical point and spills into GPi
 - Positive feedback
 - Volitional commitment to a reaching action

Recurrent attractor model





Thura & Cisek (2014) Neuron; Thura & Cisek (2016) J. Neurosci.; Thura & Cisek (2017) Neuron

Visualizing the dynamics

- Compute neural state in the high-dimensional space of recorded cells
- Extract the principal components (PCs) that capture the variance



economic and the second second



 The top four components reflect the key elements of the urgency gating model: *commitment*, *evidence*, baseline and slope of *urgency*

Visualizing the dynamics

- Trajectories in PC space
 - States during deliberation
 - "Decision manifold"



Moment of commitment



Visualizing the dynamics

- Trajectories in PC space
 - States during deliberation
 - "Decision manifold"



- Moment of commitment
- Choice-specific attractors



 Transition from deliberation to commitment is a state transition within a unified dynamical system

Unified system, but with specialization

- Different dynamics in different regions
 - Dorsal premotor cortex
 - Curved decision manifold
 - Primary motor cortex
 - Planar decision manifold



Unified system, but with specialization

- Different dynamics in different regions
 - Dorsal premotor cortex
 - Curved decision manifold
 - Primary motor cortex
 - Planar decision manifold
 - Dorsolateral prefrontal cortex
 - Extended mostly along PC2 (evidence)
 - Globus pallidus
 - Extended mostly along PC4 (urgency)
- PFC provides evidence, basal ganglia provide urgency, PMd/M1 put them together



Clinical implications?





Urgency as an individual trait



- Subjective differences
 - Feeling of effort

. . .

- Importance of time
- Different urgency signals

Subjective Risk Reward Effort Sensitivity Sensitivity (Utility x Success Probability)-Ust- C R = Reward Rate Deliberation Time + Haftdling Time + ITI Urgency **Temporal** Discounting Factor

Urgency as an individual trait

- Subjective differences
 - Feeling of effort

. . .

- Importance of time
- Different urgency signals
 - Low-urgency individual
 - High-urgency individual



Urgency as an individual trait

- Subjective differences
 - Feeling of effort
 - Importance of time
- Different urgency signals
- Free response tasks

. . .

- High-urgency \rightarrow short RT
- Low-urgency \rightarrow long RT
- Fixed duration tasks
 - High-urgency \rightarrow fast mvmt
 - Low-urgency \rightarrow slow mvmt



Individual differences

- Those who move with more vigor tend to respond more quickly
 - Jaśkowski et al. 2000; Reppert et al. 2018
- These traits are stable, and can be used to identify individuals
 - Choi et al. 2014; Reppert et al. 2015; Rigas et al. 2016; Bargary et al. 2017; Friedman et al. 2017; Berret et al. 2018
- "Impulsive" individuals
 - Make decisions quickly (Burnett-Heyes et al. 2012; Voon et al. 2014)
 - Have trouble withholding responses (Aichert et al. 2012; Choi et al. 2014; Speiser et al. 2017)
 - Sensation-seeking, prone to boredom (Watt & Vodanovich 1992; Whiteside & Lynam 2001; Berret et al. 2018)
 - Steeper temporal discounting (Shadmehr et al. 2010; Haith et al. 2012; Dalley & Robbins 2017; Summerside et al. 2018)
- "Conservative" individuals

Parkinson's Disease (PD)

Bradykinesia

- Slowing, but not an inability to move (Mazzoni et al. 2007)
- Insufficient modulation of motor system by reward (Pekny et al. 2015)
- Proposal: Pathologically *diminished* urgency
- Therapy (dopamine replacement, DBS)
 - Significantly exaggerated temporal discounting (Housden et al. 2010)
 - Symptoms of trait impulsivity (Djamishidian et al. 2014; Kojovic et al. 2016; Frank et al. 2007)
 - Prolonged treatment can lead to mania and impulse control disorders (Maier et al. 2014; Lopez et al. 2017; Molina et al. 2000; Seedat et al. 2000)
 - Proposal: Pathologically *elevated* urgency
Major Depressive Disorder (MDD)

Affective symptoms

- Non-affective symptoms
 - "Activational" aspects of motivation
 - Low energy, apathy, and fatigue
 - Psychomotor slowing, neurocognitive retardation
 - Less sensitivity to rewards, less willing to exert effort for rewards, experience greater subjective difficulty in producing force
 - High comorbidity with Parkinson's (Koerts et al. 2007; Rana et al. 2015)
 - Not alleviated by SSRI treatments of the affective symptoms of MDD (Stahl 2002; Treadway & Zald 2011; Fava et al. 2014; Gorwood et al. 2014)
 - Instead, they are more responsive to *noradrenaline* and *dopamine* reuptake inhibitors (NDRIs) (Pae et al. 2007; Stahl 2002; Treadway & Zald 2011; Zisook et al. 2006; Demyttenaere et al. 2005; Stahl et al. 2003)
 - Proposal: Pathologically *diminished* urgency
 - Absence of these symptoms (intact urgency?) is often a predictor of response to SSRI treatment

A "dimensional" view of urgency

Carland, Thura & Cisek (2019) The Neuroscientist



- A continuum of variation in urgency/vigor across individuals
- The extrema correspond to pathologies
- Reward rate → neural mechanisms → psychological phenomena

Conclusions

- Need to move beyond the drift-diffusion model
 - Accumulation of *novel* evidence, resembling a low-pass filter with a short time constant
 - Urgency signal pushes activity to commitment, implementing a decreasing accuracy criterion
- Urgency is an individual trait
 - Too high: impulse control disorders, ADHD, mania
 - Too low: bradykinesia, psychomotor slowing, motivational aspects of depression
- Dynamical system for dynamic decisions
 - Cerebral cortex implements the evolving deliberation
 - Basal ganglia energize the decision, confirm commitment, and invigorate the action
 - Decisions are made through recurrent attractor dynamics

Thank you

"The great end of life is not knowledge but action" T. H. Huxley (1825-1895)



"Your head is there to move you around" R.E.M. (1980-2011)

Current lab members

- Marie-Claude Labonté (technician)
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